

# Symbolic Execution and Program Testing

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PRESENTED BY: MENG WU


# History of Symbolic Execution

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- Robert S. Boyer, Bernard Elspas, and Karl N. Levitt. SELECT—a formal system for testing and debugging programs by symbolic execution. In ICRS, pages 234–245, 1975.
- James C. King. Symbolic execution and program testing. CACM, 19(7):385–394, 1976. (most cited)
- Leon J. Osterweil and Lloyd D. Fosdick. Program testing techniques using simulated execution. In ANSS, pages 171–177, 1976.
- William E. Howden. Symbolic testing and the DISSECT symbolic evaluation system. IEEE Transactions on Software Engineering, 3(4):266–278, 1977.

# About the Paper

## Symbolic execution and program testing

Full Text:  PDF

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Published in:



· Magazine  
Communications of the ACM [CACM Homepage](#) [archive](#)  
Volume 19 Issue 7, July 1976  
Pages 385-394  
[ACM](#) New York, NY, USA  
[table of contents](#) doi> [10.1145/360248.360252](https://doi.org/10.1145/360248.360252)



1976 Article



### [Bibliometrics](#)

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- Citation Count: 528

# Problems in Program Testing

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Predicates



Program



Assertion

Req1: enumerate all possible input values

Req2: explore all feasible paths

# Problems in Program Testing

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Predicates

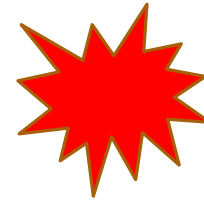


Program

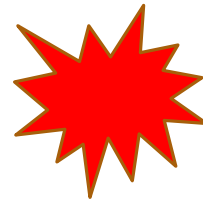


Assertion

Req1: enumerate all possible input values



Req2: explore all feasible paths



# Problems in Program Testing

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Predicates



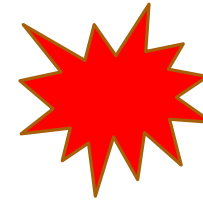
Program



Assertion

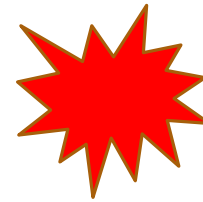
Req1: enumerate all possible input values

Symbolic Execution



Req2: explore all feasible paths

BMC or Abstraction



# Main Ideas

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- Generalize testing by using unknown symbolic variables in evaluation
- Update a symbolic state formula after each statement
- Check the path constrains/conditions

# Main Ideas

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## Insights:

- 'Execute' programs with symbols: track symbolic state rather than concrete input
- 'Execute' many program paths simultaneously: when execution path diverges, fork and add constraints on symbolic values
- When 'execute' one path, we actually simulate many test runs, since we are considering all the inputs that can exercise the same path



# Example

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WIKIPEDIA  
The Free Encyclopedia

## Example [\[edit\]](#)

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Consider the program below, which reads in a value and fails if the input is 6.

```
y = read()
y = 2 * y
if (y == 12)
    fail()
print("OK")
```

- Manual test creation: build test with input 6
- Auto-Test?
  - $y$  is 32-bit integer
  - How many test inputs for full coverage?  $2^{32}$

# Example

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## Example [\[edit\]](#)

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Consider the program below, which reads in a value and fails if the input is 6.

```
y = read()  
y = 2 * y  
if (y == 12)  
    fail()  
print("OK")
```

**y is symbolic:  $y = s$**

**$y = 2 * s$  // still symbolic**

Fork execution, add constraints to each path

**true path constraint:**

**$2*s==12$**

**Need constraint solver**



That`s all you need to know!

# More Details

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- Definition: execution state
  - Line number
  - values of variables (symbolic/concrete):  $x=s_1, y=s_2+3*s_4$
  - Path Condition (PC): conjunction of constraints (boolean formulas) over symbols:  
 $s_1>0 \wedge \alpha_1+2*s_2>0 \wedge \neg(s_3>0)$

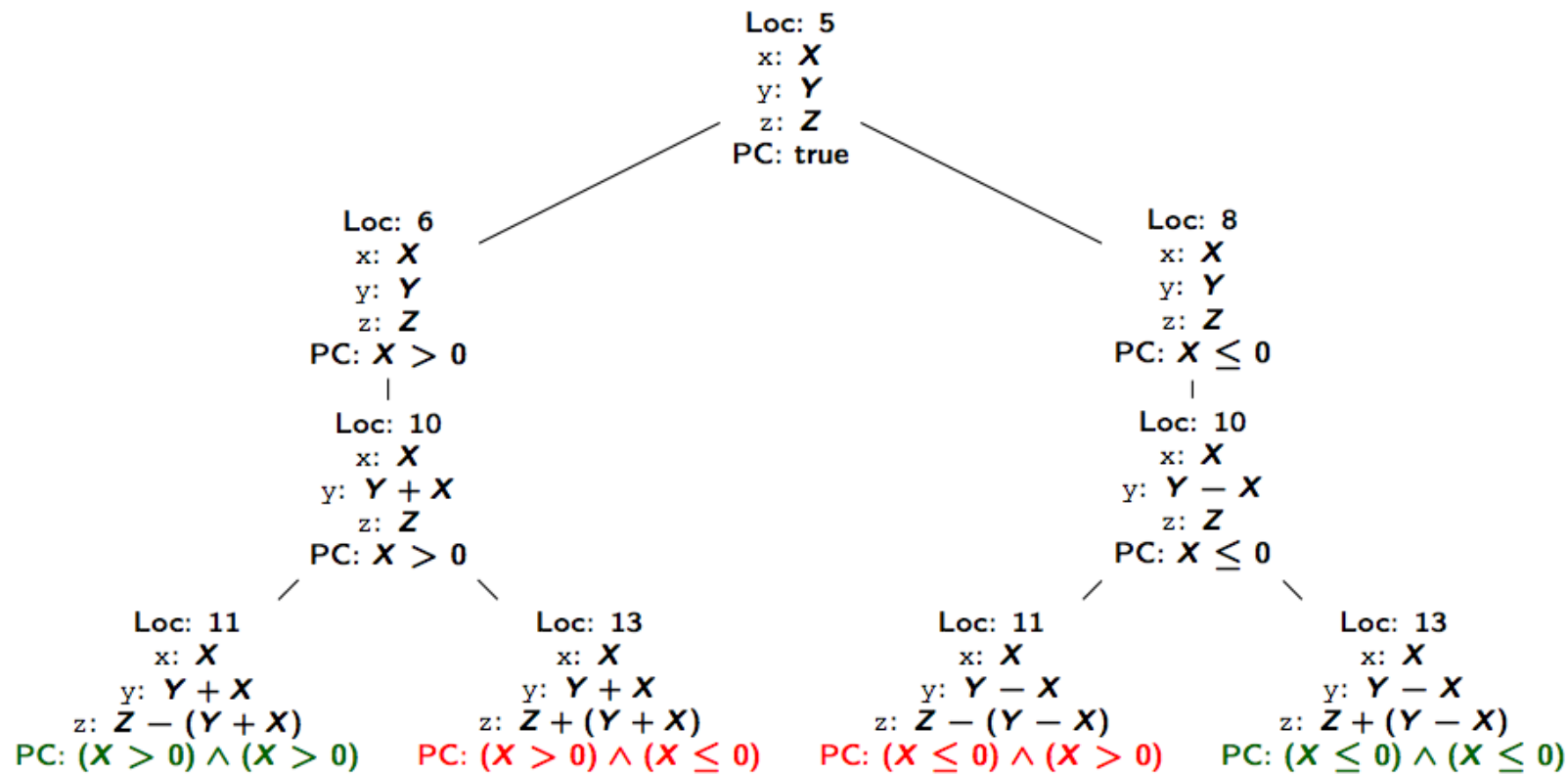
# More Details

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- Execute assignment: evaluate RHS symbolically, assign to LHS as part of the the state.
- Execute IF (r) / then / else: fork
  - then:  $PC \leftarrow PC \wedge r$
  - else:  $PC \leftarrow PC \wedge \neg r$
- Termination: solve constraint

# Execution tree

```
1 int y;  
2 int z;  
3 ...  
4 int foo(int x) {  
5     if (x > 0) {  
6         y = y + x;  
7     } else {  
8         y = y - x;  
9     }  
10    if (x > 0) {  
11        z = z - y;  
12    } else {  
13        z = z + y;  
14    }  
15 }
```



# Execution tree properties

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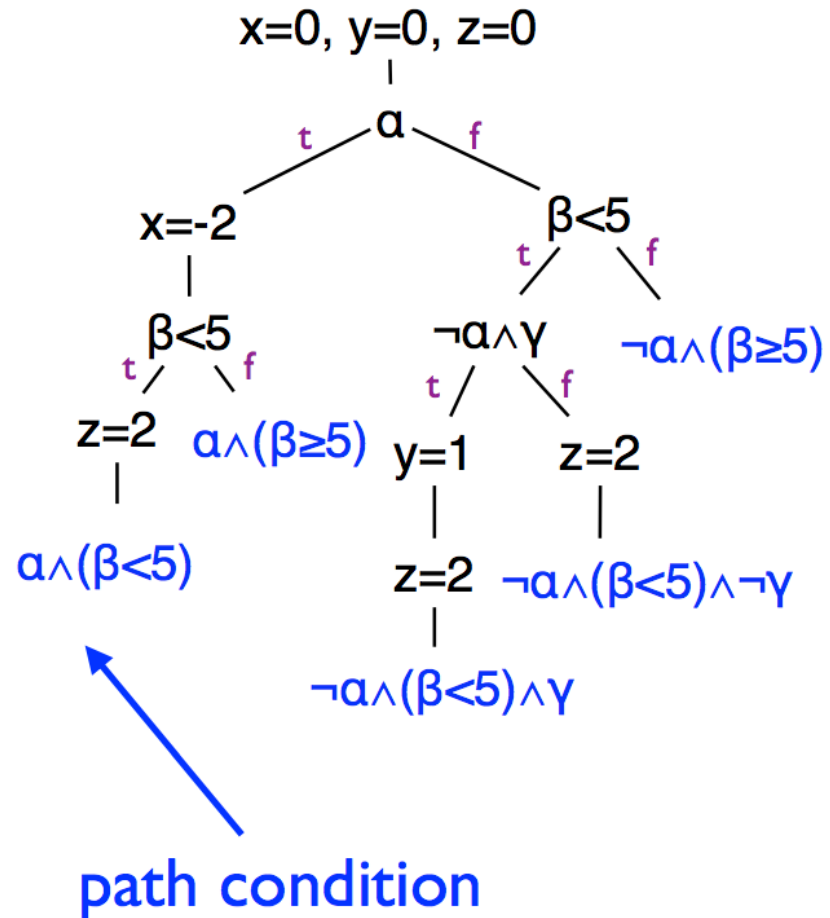
- For each satisfiable leaf exists a concrete input for which the real program will reach same leaf  $\Rightarrow$  can generate test

## Comutativity

- PC's associated with any two **satisfiable** leaves are distinct  $\Rightarrow$  code coverage.

# Applications

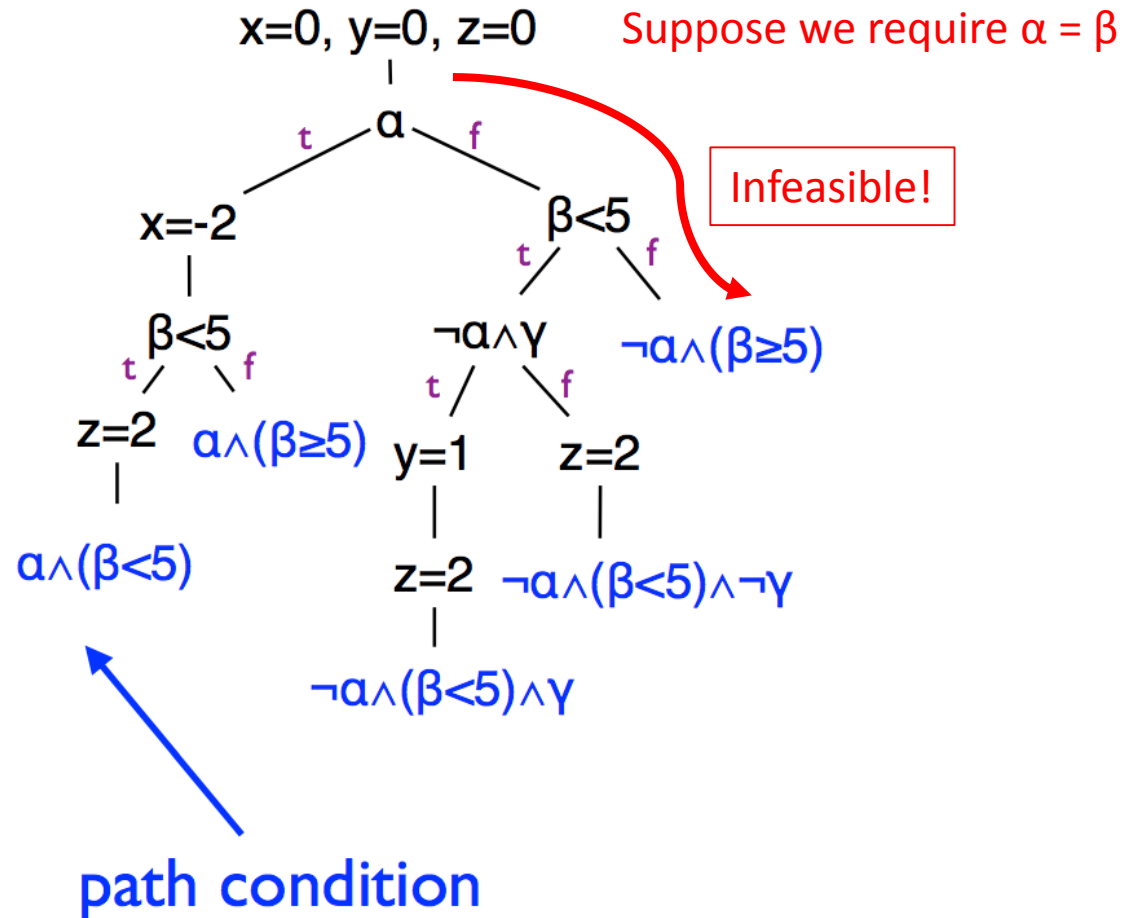
1. `int a =  $\alpha$ , b =  $\beta$ , c =  $\gamma$ ;`
2. `// symbolic`
3. `int x = 0, y = 0, z = 0;`
4. `if (a) {`
5. `x = -2;`
6. `}`
7. `if (b < 5) {`
8. `if (!a && c) { y = 1; }`
9. `z = 2;`
10. `}`
11. `assert(x+y+z!=3)`





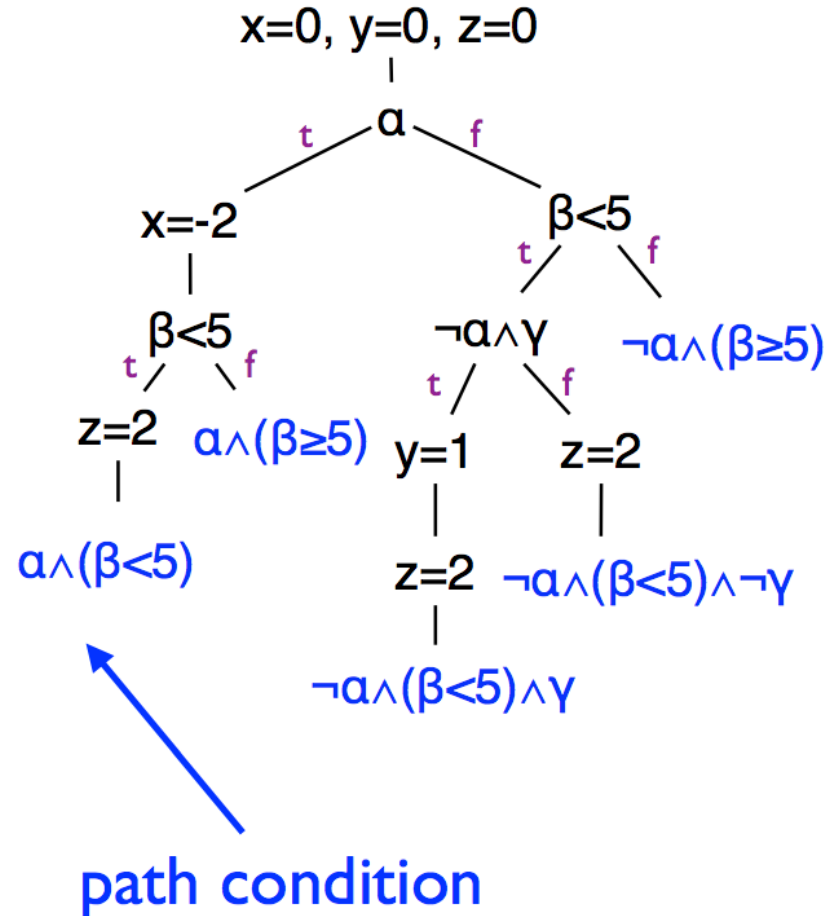
# Detecting Infeasible Paths

1. `int a =  $\alpha$ , b =  $\beta$ , c =  $\gamma$ ;`
2. `// symbolic`
3. `int x = 0, y = 0, z = 0;`
4. `if (a) {`
5. `x = -2;`
6. `}`
7. `if (b < 5) {`
8. `if (!a && c) { y = 1; }`
9. `z = 2;`
10. `}`
11. `assert(x+y+z!=3)`



# Test Input Generation

1. `int a =  $\alpha$ , b =  $\beta$ , c =  $\gamma$ ;`
2. `// symbolic`
3. `int x = 0, y = 0, z = 0;`
4. `if (a) {`
5. `x = -2;`
6. `}`
7. `if (b < 5) {`
8. `if (!a && c) { y = 1; }`
9. `z = 2;`
10. `}`
11. `assert(x+y+z!=3)`



Given Path Condition to Constrain Solver, it will produce test input for each path:

- Path 1:**  $\alpha = 1, \beta = 1$
- Path 2:**  $\alpha = 1, \beta = 6$
- Path 3 ...**

# Bug Finding

```
int foo(int i){  
    int j = 2*i;  
    i = i++;  
    i = i * j;  
    if ( i < 1 )  
        i = -i;  
    i = j/i;  
    return i;  
}
```

$i_{input}$       **$i_{input} = -1$  Trigger the bug**

**True branch:**

$$2 * i_{input}^2 + 2 * i_{input} < 1$$

$$i = - 2 * i_{input}^2 - 2 * i_{input}$$

$$i == 0$$

**False Branch: always safe**

$$2 * i_{input}^2 + 2 * i_{input} \geq 1$$

$$i = 2 * i_{input}^2 + 2 * i_{input}$$

$$i == 0$$

# A Simple Symbolic Executor: EFFIGY

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Integer Value only

IF, THEN, ELSE, DO, GO-TO, DO WHILE

Basic Operators

State Saving and Restore

Completely User Guided Execution

# Modern Tools

## Tools [\[edit\]](#)

Tool	It can analyze Arch/Lang	url	Can anybody use it/ Open source/ Downloadable
KLEE	LLVM	<a href="http://klee.github.io/">http://klee.github.io/</a> 	yes
FuzzBALL	VineLL/native	<a href="http://bitblaze.cs.berkeley.edu/fuzzball.html">http://bitblaze.cs.berkeley.edu/fuzzball.html</a> 	yes
JPF	java	<a href="http://babelfish.arc.nasa.gov/trac/jpf">http://babelfish.arc.nasa.gov/trac/jpf</a> 	yes
jCUTE	java	<a href="https://github.com/osl/jcute">https://github.com/osl/jcute</a> 	yes
Janala2	java	<a href="https://github.com/ksen007/janala2">https://github.com/ksen007/janala2</a> 	yes
KeY	java	<a href="http://www.key-project.org/">http://www.key-project.org/</a> 	yes
S2E	llvm/qemu/x86	<a href="http://dslab.epfl.ch/proj/s2e">http://dslab.epfl.ch/proj/s2e</a> 	yes
Pathgrind <sup>[4]</sup>	native 32bit valgrind based	<a href="https://github.com/codelion/pathgrind">https://github.com/codelion/pathgrind</a> 	yes
Mayhem	binary	<a href="http://forallsecure.com/mayhem.html">http://forallsecure.com/mayhem.html</a> 	no
Otter	C	<a href="https://bitbucket.org/khooy/otter/overview">https://bitbucket.org/khooy/otter/overview</a> 	yes
SymDroid	Dalvik bytecode	<a href="http://www.cs.umd.edu/~jfooster/papers/symdroid.pdf">http://www.cs.umd.edu/~jfooster/papers/symdroid.pdf</a> 	no
Rubyx	Ruby	<a href="http://www.cs.umd.edu/~avik/papers/ssarorwa.pdf">http://www.cs.umd.edu/~avik/papers/ssarorwa.pdf</a> 	no
Pex	.NET Framework	<a href="http://research.microsoft.com/en-us/projects/pex/">http://research.microsoft.com/en-us/projects/pex/</a> 	no
Jalangi	JavaScript	<a href="https://github.com/SRA-SiliconValley/jalangi">https://github.com/SRA-SiliconValley/jalangi</a> 	yes
Kite	llvm	<a href="http://www.cs.ubc.ca/labs/isd/Projects/Kite/">http://www.cs.ubc.ca/labs/isd/Projects/Kite/</a> 	yes
pysymemu	amd64/native	<a href="https://github.com/feliam/pysymemu/">https://github.com/feliam/pysymemu/</a> 	yes
Triton	x86-64	<a href="http://triton.quarkslab.com">http://triton.quarkslab.com</a> 	yes
angr	libVEX based	<a href="http://angr.io/">http://angr.io/</a> 	yes

# Problems And Later Research

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- Path Explosion (IF, Loops)

Search Strategy: Random Search, Coverage Guided Search

Concolic (concrete&symbolic) Testing

- Constrain Solving

Powerful SAT/SMT solver: Z3, STP, Yices

Non-linear Constrains, Float-point constrains, Quantifiers, Disjunction

- Memory Modeling

KLEE : Open source symbolic executor; Runs on top of LLVM

- Handling Concurrency

# Thanks & Questions?

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Reference:

Symbolic Execution for Software Testing: Three Decades Later”, CACM, Feb 2013, p 82-90

<https://www.cs.umd.edu/class/fall2011/cmsc631/>

<http://www.seas.harvard.edu/courses/cs252/2011sp>

[https://en.wikipedia.org/wiki/Symbolic\\_execution](https://en.wikipedia.org/wiki/Symbolic_execution)